

Tensor Reggeons from Warped Space at the LHC

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Title Explanation

Tensor Reggeons from Warped Space at the LHC

- Tensor means Spin 2 particles;
- Reggeons means String-inspired;
- Warped means Randall-Sundrum;
- LHC means Large Hot Chocolate.

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Outline

- 1 Background: Strings at the LHC
- 2 An Effective Field Theory
 - Matching to String Theory
 - Kaluza-Klein Decomposition
- 3 Phenomenology
- 4 Future Directions

TeV-Scale Gravity

There are two different conceptions of the traditional Hierarchy Problem. They lead to two different types of solution:

- Why is Λ_{SM} so small? \longrightarrow Raise cut-off scale.
 - Supersymmetry, Little Higgs Theories, Technicolour, ...
- Why is M_{Pl} so large? \longrightarrow Lower scale of gravity.
 - Large Extra Dimensions (Arkani-Hamed, Dimopoulos & Dvali models)
 - Warped Extra Dimensions (Randall-Sundrum models)

The second class of solutions imply gravity at the LHC!

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Quantum Gravity at the LHC

TeV-scale gravity as an effective field theory:

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_n \frac{c_n}{(M_{grav})^n} \mathcal{O}_n.$$

For $E \gtrsim M_{grav}$, we need to know **all** the c_n !

We need the UV completion;
but the cupboard of quantum gravity is pretty bare.

Perhaps the best motivated framework is String Theory.

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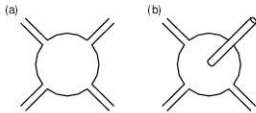
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String Theory at the LHC

The Usual Approach

String Theory at the LHC has been looked at previously:



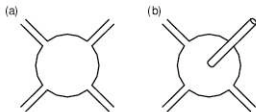
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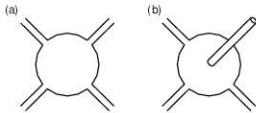
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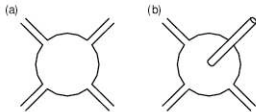
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Unfortunately, String Theory in RS not currently calculable. :(

(See Reece, Wang: 1003.5669[hep-ph]).

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I am a free man!

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Plan

- 1 Identify characteristically Stringy phenomena.
 - High spin Regge resonances \rightarrow Reggeons!
- 2 Construct flat-space EFT to describe them.
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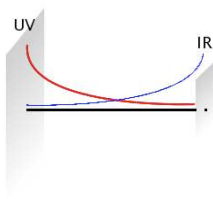
Randall-Sundrum: A Refresher and Notation

RS Models are 5D orbifolds with a non-trivial warped geometry.

$$ds^2 = e^{-2k|y|} dx^\mu dx_\mu - dy^2; \quad y \sim -y.$$

Define IR scale $\Lambda_{IR} \equiv k e^{-k\pi R}$.

UV Scales: $k \ll M_S \ll M_{Pl}$; $k \sim M_{Pl}/10$.



- SM states are zero modes of five dimensional fields;

- First “Higgsed” Model:

- $\Lambda_{IR} \sim 1 \text{ TeV}$;
- Fermions are localised in XD.

- Second “Higgsless” Model

- $\Lambda_{IR} \sim 500 \text{ GeV}$;
- Fermions are flat in XD.

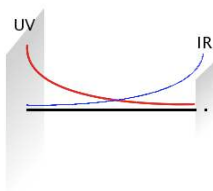
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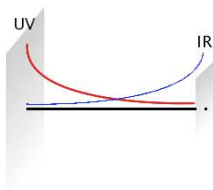
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Regge Resonances in Flat Space

General result in flat space:

$$\mathcal{A}_{str} \sim \mathcal{A}_{SM} \times \mathcal{S}(s, t).$$

$\mathcal{S}(s, t)$ is Veneziano amplitude:

$$\mathcal{S}(s, t) = \frac{\Gamma(1 - \alpha' s) \Gamma(1 - \alpha' t)}{\Gamma(1 - \alpha' s - \alpha' t)}.$$

This has infinite set of poles at $\alpha' s = n$ for $n \geq 1$.

Near n th pole, can reproduce string amplitudes with particles of mass $n/\alpha' \equiv nM_S^2$.

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Regge Resonances in Flat Space II

Cullen, Peskin & Perelstein, hep-ph/0001166.

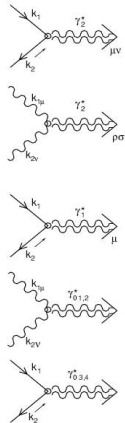
In 4d flat space Stringy QED, find at $n = 1$:

- One spin two state;
- One vector state;
- Several Scalars.

First state is most interesting:
 Unusually high spin.

All interactions determined by:

- Gauge coupling e ;
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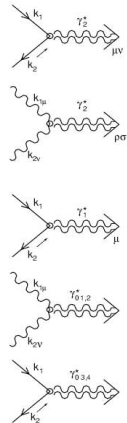
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Regge Resonances in Curved Space

Effective Theory of Spin-2 Gluon Partner:

$$\mathcal{L} = \mathcal{L}_{free} + \frac{g_s}{\sqrt{2}M_S} \left(F^{\mu\rho} F_{\rho}^{\nu} - \frac{1}{4} F^{\rho\sigma} F_{\rho\sigma} \eta^{\mu\nu} \right) B_{\mu\nu} \\ + \frac{ig_s}{\sqrt{2}M_S} (\partial_{\mu} \bar{Q} \gamma_{\nu} q - \bar{Q} \gamma_{\nu} \partial_{\mu} q) B^{\mu\nu}.$$

To produce our ‘RS String Model’ we take the above and:

- Extend to 5D (trivial);
- Covariantly generalise (tricky);
 - Limitation: don't know that Reggeon masses still M_S !
 - Limitation: lose any curvature-dependent interactions!
- Integrate over extra dimension (simple).

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Massive Spin-2 Fields in RS

A Small Digression

In flat space:

$$\mathcal{L} = \frac{1}{4}H_{\mu\nu\rho}H^{\mu\nu\rho} - \frac{1}{2}H_{\mu\nu}{}^{\nu}H^{\mu\rho}{}_{\rho} + \frac{1}{2}m^2((B_{\mu}{}^{\mu})^2 - B_{\mu\nu}B^{\mu\nu}).$$

Field Strength Tensor:

$$H_{\mu\nu\rho} \equiv \partial_{\mu}B_{\nu\rho} - \partial_{\nu}B_{\mu\rho}.$$

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Correct generalisation to RS space is non-trivial:

$$\eta_{\mu\nu} \rightarrow g_{MN}; \quad \partial_\mu \rightarrow \nabla_M; \quad B_{\mu\nu}(y) = B_{\mu\nu}(-y);$$

$$\Delta\mathcal{L} = \frac{3}{2} k^2 ((B_M{}^M)^2 - B_{MN} B^{MN}) - k \partial_y \text{sgn}(y) ((B_\mu{}^\mu)^2 - B_{\mu\nu} B^{\mu\nu}).$$

The last term comes from expanding the Einstein-Hilbert action.

Four-Dimensional Decomposition

Have now produced our 5D “String” theory. So the question is:

What are the **4D** physics?

States we expect:

$$B_{\mu\nu} \rightarrow 4\text{D Spin } 2; \quad B_{\mu y} \rightarrow 4\text{D Spin } 1; \quad B_{yy} \rightarrow 4\text{D Spin } 0.$$

Continue to focus on Spin 2 state:

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 \implies light compared to vector.

Note: Scalar also even under orbifold symmetry;

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Eliminating Mixing Terms

Problem: $B_{\mu\nu}$ contains **vector**, **scalar** components:

$$B_{\mu\nu} \sim B_{\mu\nu}^{(n)} + (\partial_\mu A_\nu^{(n)} - \partial_\nu A_\mu^{(n)}) + \dots$$

Equivalently, the action is not diagonal from the 4D perspective:

$$\mathcal{L} \supset \partial_\mu B^{\mu\nu} \partial_\nu B_{\mu\nu}.$$

Solution: Two different methods, lead to same result.

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The KK Spectrum I

Equation of Motion

So, isolating the tensor components of the free action:

$$\mathcal{L}_{4D} = \int dy \left[e^{2k|y|} \left(\frac{1}{4} H_{\lambda\mu\nu} H^{\lambda\mu\nu} - \frac{1}{2} H^{\lambda\mu}{}_{\mu} H_{\lambda\nu}{}^{\nu} \right) + \frac{1}{2} B_{\mu}{}^{\mu} \mathcal{D} B_{\nu}{}^{\nu} - \frac{1}{2} B_{\mu\nu} \mathcal{D} B^{\mu\nu} \right].$$

The mass operator \mathcal{D} is

$$\mathcal{D} \equiv -\partial_y^2 + 4k^2 + m^2 - 2k \partial_y \operatorname{sgn}(y).$$

Note: Eigenvalue equation is

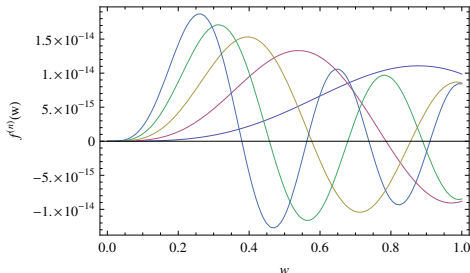
$$\mathcal{D} f^{(n)} = \mu^{(n)2} e^{2k|y|} f^{(n)},$$

with $\partial_y(e^{2k|y|} f^{(n)})$ continuous at the boundaries.

The KK Spectrum II

KK Functions

The solutions for $f^{(n)}$ are Bessel functions:



$$f^{(n)}(y) = \frac{1}{N} \left\{ J_\nu \left(\frac{\mu^{(n)}}{\Lambda_{IR}} w \right) + c J_{-\nu} \left(\frac{\mu^{(n)}}{\Lambda_{IR}} w \right) \right\};$$

$$w = e^{k(|y| - \pi R)} \in [e^{-k\pi R}, 1],$$

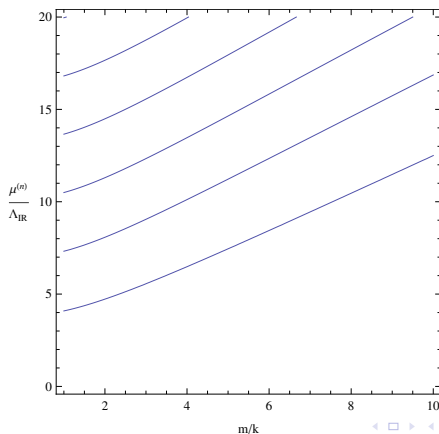
$$\nu \equiv \sqrt{4 + m^2};$$

$$N \sim \frac{e^{k\pi R}}{\sqrt{k\pi R}}; \quad c \sim e^{-2\nu k\pi R}.$$

The KK Spectrum III

Reggeon Masses

The Lightest Reggeon has mass (a few) $\times \frac{m}{k} \Lambda_{IR}$:



Reggeon-Standard Model Interactions

In 4D theory, all interactions have flat space form.

Only difference is **Overlap Integral**.

Example: Quark-Quark-Reggeon coupling,

$$\mathcal{L}_{q\bar{q}g^*} = \sum_n \frac{ig_s \tilde{g}_i^{(n)}}{\sqrt{2\tilde{M}_S}} \left(\partial^\mu \bar{q} \gamma^\nu \tilde{B}_{\mu\nu} q - \bar{q} \gamma^\nu \tilde{B}_{\mu\nu} \partial^\mu q \right).$$

\tilde{M}_S is warped-down string scale:

$$\tilde{M}_S = e^{-k\pi R} M_S \sim \text{a few TeV},$$

while $\tilde{g}_i^{(n)}$ is KK wavefunction integral:

$$\tilde{g}_i^{(n)} = e^{-k\pi R} \int_0^{\pi R} dy e^{-k|y|} f^{(n)} Q_i^{(0)2}.$$

Overlap Integrals

Table of effective couplings:

$\frac{m}{k}$	$\frac{\mu^{(0)}}{\Lambda_{\text{IR}}}$	\tilde{g}_{Glu}	$\tilde{g}^{(0)}(c = 0.65)$	$\tilde{g}^{(0)}(c = 0.5)$	$\tilde{g}^{(0)}(c = 0)$
2.0	4.72	0.110	3.9×10^{-5}	0.110	2.9
3.0	5.56	0.107	3.8×10^{-5}	0.107	2.9
4.0	6.48	0.104	3.7×10^{-5}	0.104	2.9
5.0	7.45	0.100	3.5×10^{-5}	0.100	2.8

Cross Sections and Decay Rates

Figure: Production Cross Section

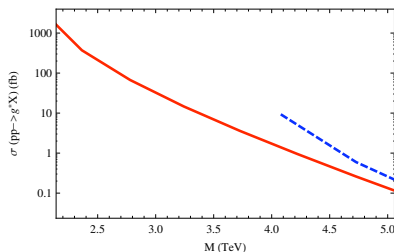
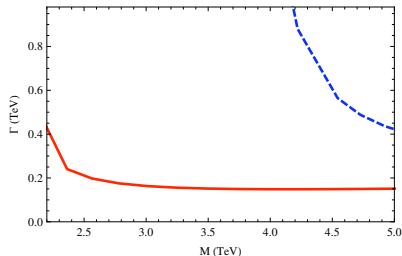


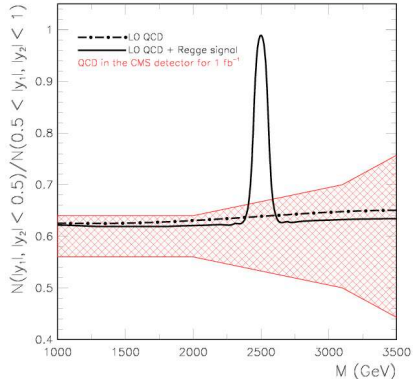
Figure: Decay Width (to SM)



Red Lines: Higgsless Model. Blue Lines: Higgsed Model.
Branching fraction over 95% to Top Quarks.

A Proper Collider Study

A follow-up paper by Anchordoqui *et. al.* looked at detection prospects: [arXiv:1006.3044]



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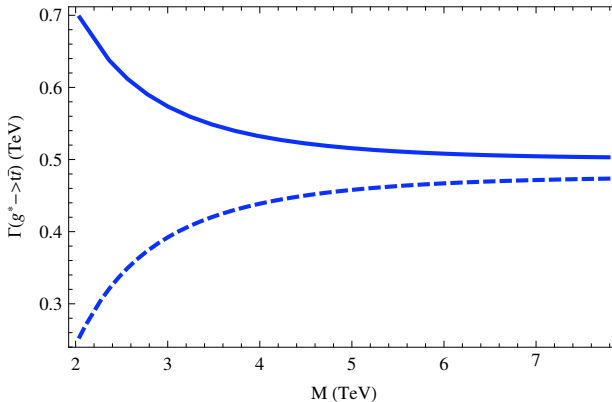
Reggeon has spin 2.

⇒ Measure spin, either **Reggeon** or **KK Graviton**.

Doubly hadronic top decays allow “full” reconstruction of momentum, measure spin from this.

New Decay Modes

All studies so far have considered decays to SM **ONLY**.
Decays to other RS states possible (KK excitations).



Summary & Conclusions

- 1 RS models imply **Stringy physics** at the LHC;
- 2 We have constructed a string-inspired **Reggeon** model;
- 3 We expect up to **1000s** of Reggeons at the LHC;
- 4 We hope to identify the Reggeons via **cascade decays**.